

University of Groningen

## Infrared signatures of the spin-Peierls transition in CuGeO<sub>3</sub>

Damascelli, A; vanderMarel, D; Parmigiani, F; Dhahlenne, G; Revcolevschi, A

*Published in:*  
Physical Review B

*DOI:*  
[10.1103/PhysRevB.56.R11373](https://doi.org/10.1103/PhysRevB.56.R11373)

**IMPORTANT NOTE:** You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

*Document Version*  
Publisher's PDF, also known as Version of record

*Publication date:*  
1997

[Link to publication in University of Groningen/UMCG research database](#)

### *Citation for published version (APA):*

Damascelli, A., vanderMarel, D., Parmigiani, F., Dhahlenne, G., & Revcolevschi, A. (1997). Infrared signatures of the spin-Peierls transition in CuGeO<sub>3</sub>. *Physical Review B*, 56(18), 11373-11376.  
<https://doi.org/10.1103/PhysRevB.56.R11373>

### **Copyright**

Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

The publication may also be distributed here under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license. More information can be found on the University of Groningen website: <https://www.rug.nl/library/open-access/self-archiving-pure/taverne-amendment>.

### **Take-down policy**

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

*Downloaded from the University of Groningen/UMCG research database (Pure): <http://www.rug.nl/research/portal>. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.*

# Infrared signatures of the spin-Peierls transition in $\text{CuGeO}_3$

A. Damascelli and D. van der Marel

*Solid State Physics Laboratory, University of Groningen, Nijenborgh 4, 9747 AG Groningen, The Netherlands*

F. Parmigiani

*INFM and Dipartimento di Fisica, Politecnico di Milano, Piazza Leonardo da Vinci, 32-20133 Milano, Italy*

G. Dhalenne and A. Revcolevschi

*Laboratoire de Chimie des Solides, Université de Paris-sud, Bâtiment 414, F-91405 Orsay, France*

(Received 21 July 1997)

We investigated the infrared reflectivity of several Mg- and Si-substituted  $\text{CuGeO}_3$  single crystals. The temperature-dependent  $b$ -axis and  $c$ -axis optical response is reported. For  $T < T_{\text{SP}}$  we detected the activation of zone-boundary phonons along the  $b$  axis of the crystal on the pure sample and for 1% Mg and 0.7% Si concentrations. From a detailed analysis of the phonon parameters the redshift of the  $B_{2u}$  mode at  $48 \text{ cm}^{-1}$  is observed and discussed in relation to the soft mode expected to drive the spin-Peierls phase transition in  $\text{CuGeO}_3$ . Moreover, the polarization dependence of a magnetic excitation measured in transmission at  $44 \text{ cm}^{-1}$  has been investigated. [S0163-1829(97)51942-4]

In 1993,  $\text{CuGeO}_3$  was recognized, on the basis of magnetic susceptibility measurements,<sup>1</sup> as an inorganic compound showing a spin-Peierls (SP) transition. This transition consists of the lattice distortion (due to the magnetoelastic coupling between the one-dimensional spin system and the three-dimensional phonon system) that occurs together with the formation of a spin-singlet ground state and the opening of a finite energy gap in the magnetic excitation spectrum. This discovery has renewed the interest in the field of the SP phase transition, observed previously on an organic material in the 1970's,<sup>2</sup> because the availability of large high-quality single crystals of  $\text{CuGeO}_3$  makes it possible to investigate this phenomenon by a very broad variety of experimental techniques. Furthermore,  $\text{CuGeO}_3$  seems to be a good candidate for the observation of a soft mode in the phonon spectrum, upon passing through the SP transition. In fact, a well-defined soft mode is expected in those theoretical models describing an SP system in terms of a linear coupling between lattice and magnetic degrees of freedom.<sup>3,4</sup> During the last few years both the structural deformation and the spin gap have been characterized in detail by x-ray and neutron-scattering experiments.<sup>5-9</sup> So far no soft mode has yet been detected in  $\text{CuGeO}_3$ .

In this paper we present a detailed spectroscopic study of the vibrational and electronic signatures of the SP transition in pure and doped  $\text{CuGeO}_3$ . We concentrate on the nature of the transition and on the dynamical interplay between spins and phonons.

We investigated the far- and mid-infrared reflectivity ( $20\text{--}6000 \text{ cm}^{-1}$ ) of several  $\text{Cu}_{1-\delta}\text{Mg}_\delta\text{GeO}_3$  ( $\delta=0,0.01$ ) and  $\text{CuGe}_{1-x}\text{Si}_x\text{O}_3$  ( $x=0,0.007,0.05,0.1$ ) single crystals. These high-quality single crystals were grown from the melt by a floating zone technique.<sup>10</sup> Samples with dimensions of approximately  $1\times3\times6 \text{ mm}^3$  were aligned by conventional Laue diffraction and mounted in a liquid He flow cryostat to study the temperature dependence of the optical properties between 4 and 300 K. The reflectivity measurements were

performed with a Fourier transform spectrometer (Bruker IFS 113v), operating in near normal incidence configuration with polarized light in order to probe the optical response of the crystals along the  $b$  and the  $c$  axes. The absolute reflectivities were obtained by calibrating the data acquired on the samples against a gold mirror.

The number and the symmetry of the infrared active phonons expected for the high-temperature undistorted phase and the low-temperature SP phase of  $\text{CuGeO}_3$  can be obtained from a group theoretical analysis of the lattice vibrational modes. At room temperature  $\text{CuGeO}_3$  has an orthorhombic crystal structure with lattice parameters  $a=4.81$ ,  $b=8.47$ , and  $c=2.941 \text{ Å}$  and space group  $Pbmm$  or, equivalently,  $Pmma$  in standard setting.<sup>11</sup> The building blocks of the structure are edge-sharing  $\text{CuO}_6$  octahedra and corner-sharing  $\text{GeO}_4$  tetrahedra stacked along the  $c$  axis of the crystal and resulting in  $\text{Cu}^{2+}$  and  $\text{Ge}^{4+}$  chains parallel to the  $c$  axis. These chains are linked together via the O atoms [denoted as O(2)] and form layers parallel to the  $b$ - $c$  plane weakly coupled along the  $a$  axis. The irreducible representation of the optical vibrations of  $\text{CuGeO}_3$ , in setting  $Pbmm$ , for  $T > T_{\text{SP}}$  is<sup>12</sup>

$$\Gamma = 4A_g(aa,bb,cc) + 4B_{1g}(ab) + 3B_{2g}(ac) + B_{3g}(bc) \\ + 3B_{1u}(E||c) + 5B_{2u}(E||b) + 5B_{3u}(E||a),$$

corresponding to an expectation of 12 Raman active modes ( $4A_g + 4B_{1g} + 3B_{2g} + B_{3g}$ ) and 13 infrared active modes ( $3B_{1u} + 5B_{2u} + 5B_{3u}$ ). Below  $T_{\text{SP}}$  the crystal structure is still orthorhombic, but with lattice parameters  $a'=2\times a$ ,  $b'=b$ , and  $c'=2\times c$  and space group  $Bbcm$  or, equivalently,  $Cmca$  in standard setting.<sup>5,7</sup> The distortion of the lattice in the phase transition can be characterized as the dimerization of the Cu-Cu pairs along the  $c$  axis (dimerization out of phase in neighboring chains), together with the rotation of the  $\text{GeO}_4$  tetrahedra around the axis defined by the O(1) sites (rotation opposite in sense for neighboring tetrahedra).

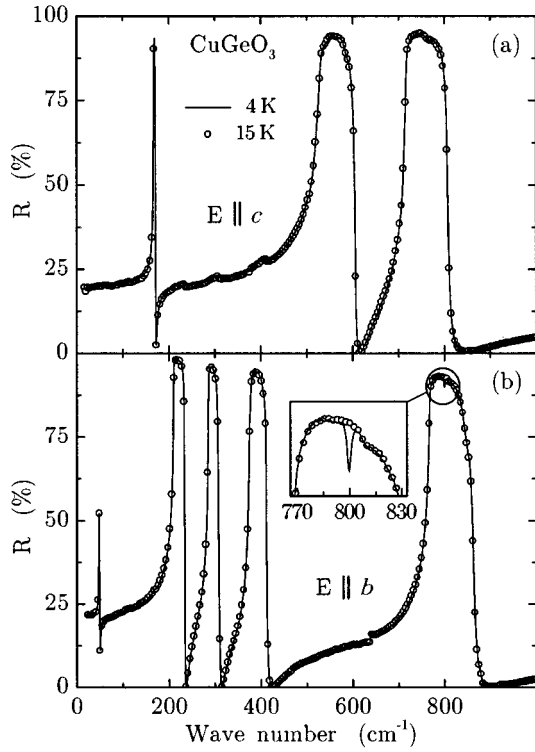


FIG. 1. Comparison between reflectivity spectra measured in the SP phase at 4 K (solid line) and just before the SP transition at 15 K (circles) on a pure single crystal of  $\text{CuGeO}_3$ . For light polarized along the  $c$  axis (a) no difference is found across the phase transition whereas for light polarized along the  $b$  axis (b) a new feature appears at  $800 \text{ cm}^{-1}$  (as clearly shown in the inset).

Moreover, the O(2) sites of the undistorted structure split in an equal number of O(2a) and O(2b) sites, distinguished by the distances O(2a)-O(2a) and O(2b)-O(2b) shorter and larger than O(2)-O(2),<sup>7</sup> respectively. The irreducible representation of the optical vibrations, in setting  $Bbcm$ , for  $T < T_{\text{SP}}$  is<sup>12</sup>

$$\Gamma_{\text{SP}} = 8A_g(aa, bb, cc) + 9B_{1g}(ab) + 7B_{2g}(ac) + 6B_{3g}(bc) \\ + 5B_{1u}(E||c) + 9B_{2u}(E||b) + 8B_{3u}(E||a).$$

Therefore 30 Raman active modes ( $8A_g + 9B_{1g} + 7B_{2g} + 6B_{3g}$ ) and 22 infrared active modes ( $5B_{1u} + 9B_{2u} + 8B_{3u}$ ) are expected for  $\text{CuGeO}_3$  in the SP phase, all the additional vibrations being zone-boundary modes activated by the folding of the Brillouin zone. In particular, the number of infrared active phonons is expected to increase from 5 to 8, 5 to 9, and 3 to 5 for light polarized along the  $a$ ,  $b$ , and  $c$  axis, respectively, upon passing through the phase transition.

The  $c$ - and  $b$ -axis reflectivity spectra of pure  $\text{CuGeO}_3$  are plotted in Fig. 1, for  $T=15 \text{ K}$  (circles) and  $T=4 \text{ K}$  (solid line). The data, characteristic of an ionic insulating material, are shown up to  $1000 \text{ cm}^{-1}$  which covers the full phonon spectrum. For  $T > T_{\text{SP}}$  three phonons are detected along the  $c$  axis ( $\omega_{\text{TO}} \approx 167, 528$ , and  $715 \text{ cm}^{-1}$  for  $T=15 \text{ K}$ ), and five along the  $b$  axis ( $\omega_{\text{TO}} \approx 48, 210, 286, 376$ , and  $766 \text{ cm}^{-1}$  for  $T=15 \text{ K}$ ), in agreement with the theoretical expectation. The structure in Fig. 1(a) between  $200$  and  $400 \text{ cm}^{-1}$  is due to a

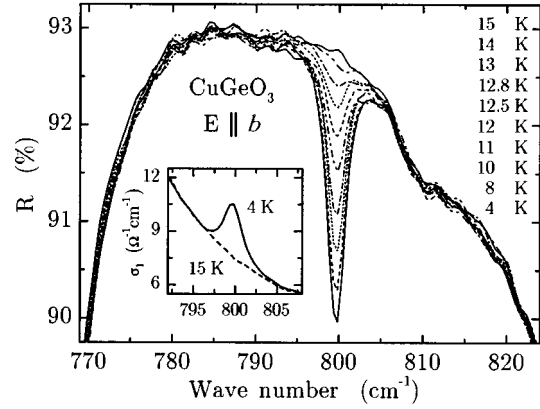


FIG. 2. Detailed temperature dependence of the feature observed with  $E||b$  in the reflectivity spectra at  $800 \text{ cm}^{-1}$  for  $T < T_{\text{SP}}$ . In the inset, where the dynamical conductivity calculated via Kramers-Kronig analysis is plotted, a new peak is clearly visible for  $T=4 \text{ K}$ .

leakage of the modes polarized along the  $c$  axis. The feature at approximately  $630 \text{ cm}^{-1}$  in Fig. 1(b) is a leakage of a mode polarized along the  $a$  axis.<sup>13</sup> Whereas for  $E||c$  the spectra are exactly identical, a new feature is detected in the SP phase at  $800 \text{ cm}^{-1}$  for  $E||b$ , as shown in the inset of Fig. 1(b). A careful investigation of temperatures ranging from 4 to 15 K (see Fig. 2) clearly shows that this feature, that falls in the frequency region of high reflectivity for the  $B_{2u}$  phonon at  $766 \text{ cm}^{-1}$  and therefore shows up in reflectivity mainly for its absorption, is activated by the SP transition. It corresponds to a new absorption peak in conductivity, superimposed on a background due to the Lorentzian tail of the close  $B_{2u}$  mode (see inset of Fig. 2). We observed the same peak (at the same resonant frequency) also on 1% Mg and 0.7% Si-doped single crystals, but not on 5 and 10 % Si-doped samples,<sup>12</sup> where we did not find any sign of the SP transition also on the basis of magnetic susceptibility measurements.

By fitting the reflectivity spectra with Lorentz oscillators for the optical phonons it is possible to obtain the temperature dependence of the oscillator strength for the  $800 \text{ cm}^{-1}$  feature. The results are plotted in Fig. 3, together with the peak intensity of the superlattice reflection measured by Harris *et al.*<sup>14</sup> in an x-ray scattering experiment on a pure  $\text{CuGeO}_3$  single crystal characterized, as our sample, by  $T_{\text{SP}} \approx 13.2 \text{ K}$ . From the perfect agreement of the infrared and x-ray scattering results on pure  $\text{CuGeO}_3$  and from the observation that the resonant frequency is not shifting at all with temperature, we can conclude that the peak at  $800 \text{ cm}^{-1}$  corresponds to a pure lattice excitation and the oscillator strength is proportional to the symmetry-breaking displacement of the atoms squared. The same conclusions can be obtained for the 1% Mg- and 0.7% Si-doped samples, where  $T_{\text{SP}}$  of approximately 12.4 and 9.3 K, respectively, are observed (in these two cases the data can be compared, for 0.7% Si doping, to those presented in Ref. 15 and, for 1% Mg doping, to those reported in Ref. 16 for a 0.9% Zn-doped sample, because no x-ray or neutron-scattering data are available in the literature for Mg-doped  $\text{CuGeO}_3$ ). Moreover, as this activated line does not show any frequency shift as a function of Si and Mg doping, we can conclude that it

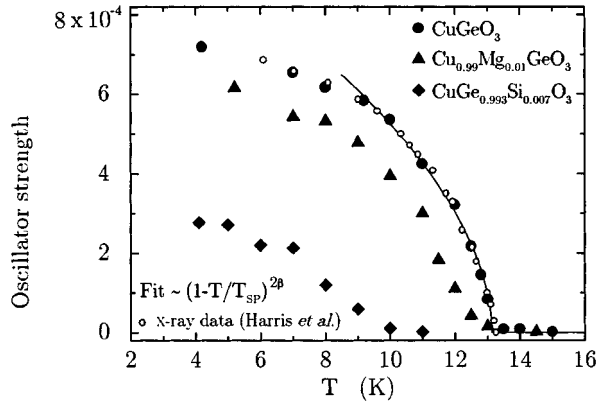


FIG. 3. Temperature dependence of the oscillator strength of the zone-boundary mode observed for  $E||b$  at  $800\text{ cm}^{-1}$  on pure (filled circles), 1% Mg-doped (triangles), and 0.7% Si-doped (diamonds)  $\text{CuGeO}_3$  single crystals. For comparison the x-ray scattering data of Harris *et al.* (Ref. 14) are also plotted (open circles).

has to be a folded zone-boundary mode related to the  $B_{2u}$  phonon observed at  $766\text{ cm}^{-1}$ , which is mainly an oxygen vibration.<sup>13</sup> This gives for the  $B_{2u}$  mode an energy dispersion, over the full Brillouin zone, of the order of  $34\text{ cm}^{-1} = 4.22\text{ meV}$  at  $T = 15\text{ K}$ .

The reasons for not observing in our reflectivity spectra for  $T < T_{\text{SP}}$  all the phonons predicted from the group theoretical analysis, are probably the small values of the atomic displacements involved in the SP transition (with a correspondingly small oscillator strength of zone-boundary modes), and/or possibly the small dispersion of the optical branches of some of the lattice vibrations. However, it is not surprising that the only activated mode has been detected along the  $b$  axis of the crystal. In fact, it is for this axis that for  $T < T_{\text{SP}}$  a spontaneous thermal contraction has been observed,<sup>17</sup> which can be responsible for a relative increase of the oscillator strength of the phonons polarized along the  $b$  axis with respect to those polarized along the  $c$  axis.

In Fig. 3 the results of a fit of the experimental data by the equation  $(1 - T/T_{\text{SP}})^{2\beta}$  over a broad temperature range are also plotted, for the pure sample. We obtained  $\beta = 0.26 \pm 0.02$  in agreement with Ref. 17. However, the best fit value of  $\beta$  is strongly dependent on the temperature range chosen to fit the data. If only points very close (within one Kelvin) to  $T_{\text{SP}}$  are considered, the value  $\beta = 0.36 \pm 0.03$  is obtained, as reported in Ref. 6. It is not possible to perform the same fit for the data acquired on doped samples because they are characterized by an upturned curvature near  $T_{\text{SP}}$ , which can be explained in terms of a distribution of transition temperatures due to the disorder introduced upon doping the system.<sup>15</sup>

As far as the dynamical interplay between spins and phonons in  $\text{CuGeO}_3$  is concerned, it is clear from the reflectivity spectra plotted in Fig. 1 that a well-defined soft mode, driving the structural deformation in  $\text{CuGeO}_3$ , has not been detected in our measurements. However, interesting information can be drawn from the temperature dependence of the phonon parameters obtained from the fit of the reflectivity data for the pure sample. In Fig. 4 the frequency shift (in percent) for the  $B_{1u}$  modes ( $E||c$ ) and the  $B_{2u}$  modes ( $E||b$ ) is plotted as a function of temperature. We can clearly observe that the  $B_{2u}$  mode at  $48\text{ cm}^{-1}$  is the only one showing

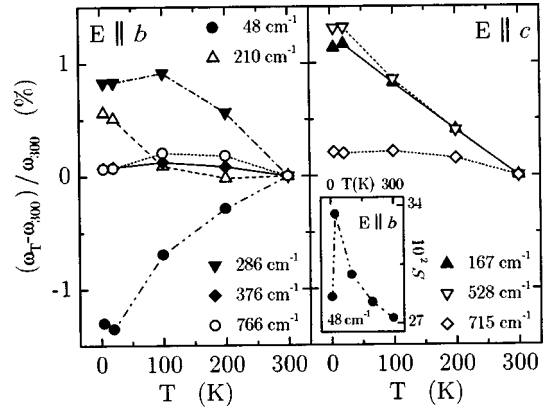


FIG. 4. Temperature dependence of the frequency shift (in percent) of the transverse optical phonons observed for  $E||b$  and  $E||c$  on the pure single crystal of  $\text{CuGeO}_3$ . In the inset the oscillator strength  $S$  of the mode detected at  $48\text{ cm}^{-1}$ , for  $E||b$ , is plotted versus the temperature.

an evident monotonic redshift from 300 to 15 K. This can be understood in terms of the normal-mode displacements obtained by Popović *et al.*<sup>13</sup> via a shell-model lattice dynamical calculation. In fact, this particular  $B_{2u}$  mode, as well as the Raman active  $B_{1g}$  at  $116\text{ cm}^{-1}$ , consists mainly of the rotation (accompanied by a slight internal distortion) of the  $\text{GeO}_4$  tetrahedra around the axis defined by the  $\text{O}(1)$  sites. It is precisely this ‘‘hinge motion’’<sup>18</sup> represented in terms of normal-mode displacements at  $k = (\pi/a, 0, \pi/c)$  which, together with the dimerization of the Cu-Cu pairs along the  $c$  axis, corresponds to the structural deformation involved in the SP phase transition. The  $B_{2u}$  mode at  $48\text{ cm}^{-1}$  has approximately the same character. Below  $T_{\text{SP}}$  this mode shows only a small blueshift. More noticeable there is a large ( $\sim 15\%$ ) reduction of oscillator strength  $S$  (see inset of Fig. 4). One may speculate at this point, that a full softening is also absent for the phonons at  $k = (\pi/a, 0, \pi/c)$ , implying that the phase transition is not driven by a softening of the phonon spectrum at  $k = (\pi/a, 0, \pi/c)$ , but by a change in electronic structure which in turn determines the dynamical charge of the ions and the interatomic force constants. In this scenario the large change in oscillator strength of some of the vibrational modes results from a change in ionicity, or, in other words, a transfer of spectral weight from the elastic degrees of freedom to electronic excitations.

A last remark has to be made regarding the temperature dependence of the  $B_{2u}$  mode ( $B_{3u}$  in standard setting) observed at  $286\text{ cm}^{-1}$ . In a recent paper<sup>19</sup> a softening of this phonon, upon going through the phase transition, was suggested. This is not confirmed by our results which show no considerable frequency shift for this resonance upon reducing the temperature from 15 to 4 K (see Fig. 4). On the other hand a reduction of both the scattering rate and the oscillator strength is observed, which can explain the double-peak structure in the reflectance ratio  $R(20\text{ K})/R(5\text{ K})$  reported in Ref. 19.

Usually in optical spectroscopy direct singlet-triplet excitations are not detectable or very weak. However, such a transition has been observed at  $44.3\text{ cm}^{-1}$  in an infrared transmission experiment where the singlet-triplet nature of the transition was demonstrated by the Zeeman splitting ob-

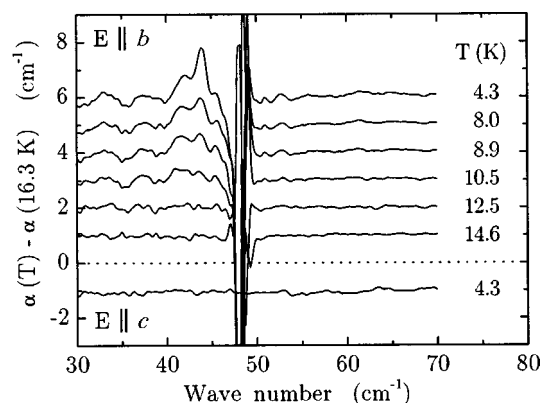


FIG. 5. Absorbance difference spectra for the pure single crystal of  $\text{CuGeO}_3$ , with  $E \parallel b$  and  $E \parallel c$ . The spectra have been shifted for clarity.

served in magnetic field.<sup>20</sup> In a very recent paper<sup>21</sup> this line was interpreted as a magnetic excitation across the gap at the wave vector  $(0, \pi/b, 0)$  in the Brillouin zone, activated by the existence of staggered magnetic fields along the  $b$  axis. In order to study this interpretation we measured the far-infrared transmission on the pure  $\text{CuGeO}_3$  single crystal for  $E \parallel b$  and  $E \parallel c$ . The absorbance difference spectra are reported in Fig. 5, where they have been shifted for clarity. For  $E \parallel c$  no absorption is observed. However, for  $E \parallel b$  an absorption

peak, showing the appropriate temperature dependence, is present at approximately  $44 \text{ cm}^{-1}$ . One has to note that the feature at  $48 \text{ cm}^{-1}$  is produced by the low-energy  $B_{2u}$  phonon. In fact, due to the strong temperature dependence of its parameters, this line does not cancel out completely in the ratios of transmission spectra measured at different temperatures. The observed polarization dependence puts a strong experimental constraint on the possible microscopic mechanism giving rise to the singlet-triplet absorption peak.

In conclusion, we have investigated the temperature-dependent phonon spectrum of pure and doped  $\text{CuGeO}_3$ , by means of infrared reflectivity measurements. We observed the activation of zone-boundary phonons along the  $b$  axis of the crystals, for  $T < T_{\text{SP}}$ , and the redshift of the  $B_{2u}$  mode at  $48 \text{ cm}^{-1}$ . The latter result has been discussed in relation to the role played by this lattice vibration in driving the system into the dimerized phase. Moreover, a magnetic excitation has been measured in transmission at  $44 \text{ cm}^{-1}$  and its polarization dependence investigated.

We gratefully acknowledge M. Mostovoi and D.I. Khomskii for stimulating discussions and T.T.M. Palstra for the magnetic susceptibility measurements. We thank P.H.M. van Loosdrecht and M. Grüninger for many useful comments. This investigation was supported by the Netherlands Foundation for Fundamental Research on Matter (FOM) with financial aid from the Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO).

<sup>1</sup>M. Hase, I. Terasaki, and K. Uchinokura, *Phys. Rev. Lett.* **70**, 3651 (1993).

<sup>2</sup>J. W. Bray, H. R. Hart, L. V. Interrante, I. S. Jacobs, J. S. Kasper, G. D. Watkins, and S. H. Wee, *Phys. Rev. Lett.* **35**, 744 (1975).

<sup>3</sup>L. N. Bulaevskii, A. I. Buzdin, and D. I. Khomskii, *Solid State Commun.* **27**, 5 (1978).

<sup>4</sup>M. C. Cross and D. S. Fisher, *Phys. Rev. B* **19**, 402 (1979).

<sup>5</sup>K. Hirota, D. E. Cox, J. E. Lorenzo, G. Shirane, J. M. Tranquada, M. Hase, K. Uchinokura, H. Kojima, H. Kojima, Y. Shibuya, and I. Tanaka, *Phys. Rev. Lett.* **73**, 736 (1994).

<sup>6</sup>M. D. Lumsden, B. D. Gaulin, H. Dabkowska, and M. L. Plumer, *Phys. Rev. Lett.* **76**, 4919 (1996).

<sup>7</sup>M. Braden, G. Wilkendorf, J. Lorenzana, M. Aïn, G. J. McIntyre, M. Behruzi, G. Heger, G. Dhalenne, and A. Revcolevschi, *Phys. Rev. B* **54**, 1105 (1996).

<sup>8</sup>O. Fujita, J. Akimitsu, M. Nishi, and K. Kakurai, *Phys. Rev. Lett.* **74**, 1677 (1995).

<sup>9</sup>M. Aïn, J. E. Lorenzo, L. P. Regnault, G. Dhalenne, A. Revcolevschi, B. Hennion, and Th. Jolicoeur, *Phys. Rev. Lett.* **78**, 1560 (1997).

<sup>10</sup>A. Revcolevschi and G. Dhalenne, *Adv. Mater.* **5**, 657 (1993).

<sup>11</sup>H. Völlenkle, A. Wittmann, and H. Nowotny, *Monatsch. Chem.* **98**, 1352 (1967).

<sup>12</sup>A. Damascelli, D. van der Marel, F. Parmigiani, G. Dhalenne, and A. Revcolevschi, *Physica B* (to be published).

<sup>13</sup>Z. V. Popović, S. D. Dević, V. N. Popov, G. Dhalenne, and A. Revcolevschi, *Phys. Rev. B* **52**, 4185 (1995).

<sup>14</sup>Q. J. Harris, Q. Feng, R. J. Birgeneau, K. Hirota, G. Shirane, M. Hase, and K. Uchinokura, *Phys. Rev. B* **52**, 15 420 (1995).

<sup>15</sup>L. P. Regnault, J. P. Renard, G. Dhalenne, and A. Revcolevschi, *Europhys. Lett.* **32**, 579 (1995).

<sup>16</sup>Y. Sasago, N. Koide, K. Uchinokura, M. C. Martin, M. Hase, K. Hirota, and G. Shirane, *Phys. Rev. B* **54**, R6835 (1996).

<sup>17</sup>Q. J. Harris, Q. Feng, R. J. Birgeneau, K. Hirota, K. Kakurai, J. E. Lorenzo, G. Shirane, M. Hase, K. Uchinokura, H. Kojima, I. Tanaka, and Y. Shibuya, *Phys. Rev. B* **50**, 12 606 (1994).

<sup>18</sup>D. Khomskii, W. Geertsma, and M. Mostovoy, *Czech. J. Phys.* **46**, 3239 (1996).

<sup>19</sup>G. Li, J. L. Musfeldt, Y. J. Wang, S. Jandl, M. Poirier, A. Revcolevschi, and G. Dhalenne, *Phys. Rev. B* **54**, R15 633 (1996).

<sup>20</sup>P.H.M. van Loosdrecht, S. Huant, G. Martinez, G. Dhalenne, and A. Revcolevschi, *Phys. Rev. B* **54**, R3730 (1996).

<sup>21</sup>G. S. Uhrig, *Phys. Rev. Lett.* **79**, 163 (1997).